



Center comparisons with survival data

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Nothing to disclose

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No conflict of interest

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Benchmarking centers

- We want to compare (the performance of) several centers with respect to some benchmark
- Often (but not always) the benchmark concerns some binary (yes/no) indicator
- The benchmark could be set at the overall rate at which the indicator occurs
- For instance, consider the indicator “bad outcome” among allogeneic transplantations
- Suppose that, among all centers, this occurs about in 25% of all allogeneic transplantations



Hypothesis test

- For now, disregard differences in case mix
 - To be discussed later
- Then, for every center we can test (with $p_0 = 0.25$)

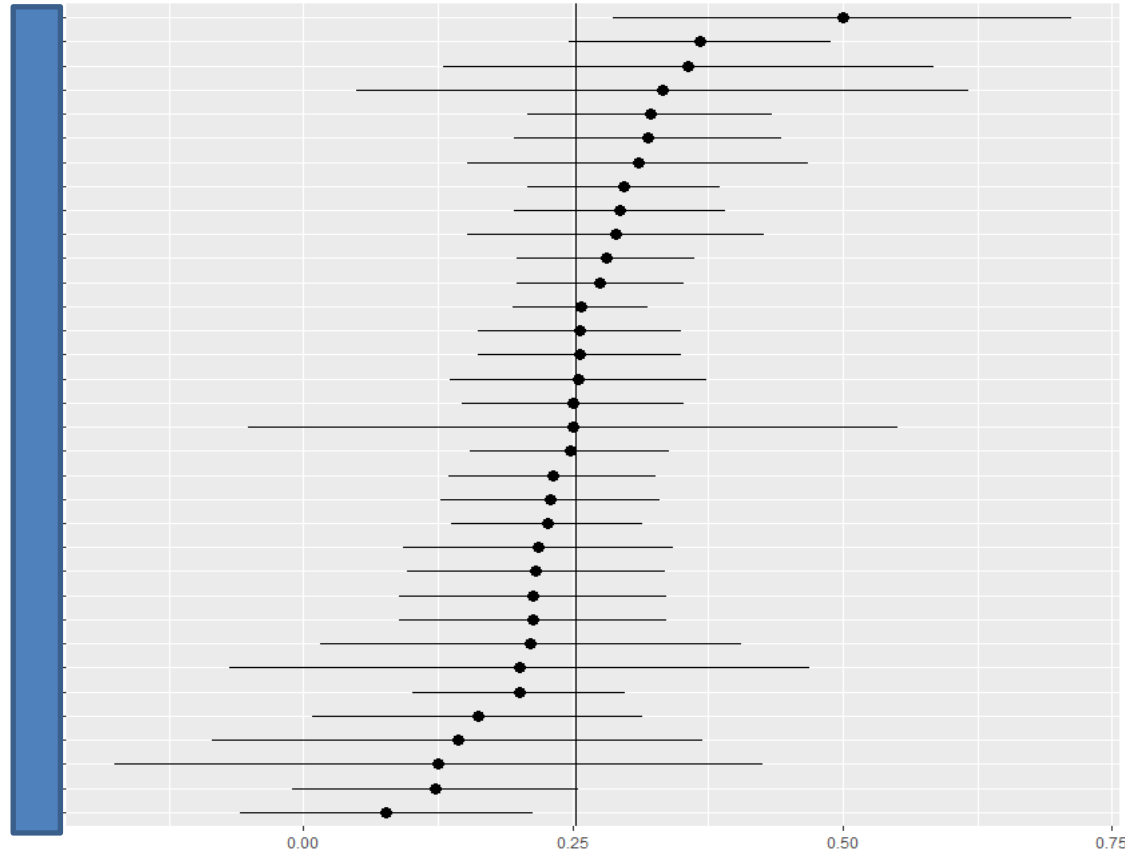
$$H_0: p = p_0 \text{ versus } H_1: p \neq p_0$$

- This is just a two-sided binomial test, and we can display results graphically in a caterpillar plot
 - Also known as league table



EBMT Caterpillar plot

- In the caterpillar plot the outcome is the estimate probability in each center
- Shown with 95% confidence intervals
- Typically ordered by effect size (or performance)



Criticizes caterpillar plots:

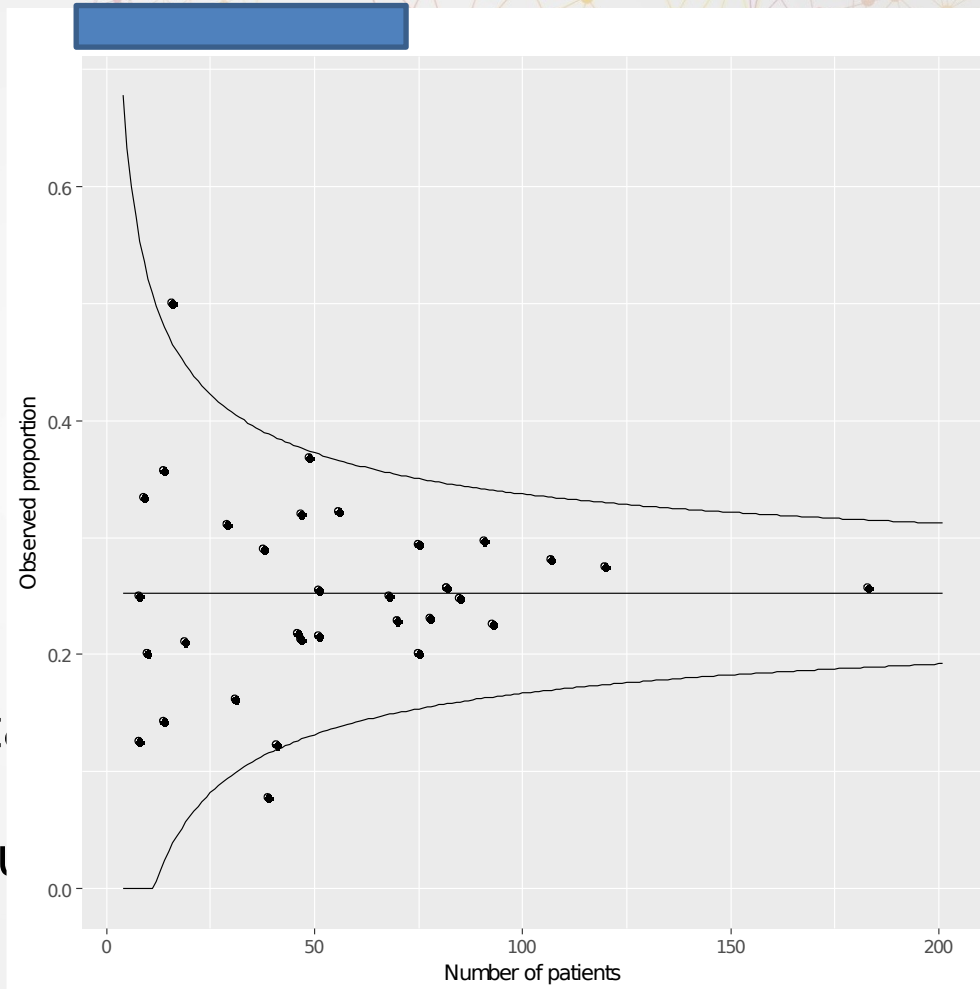
... as leading to a spurious focus on rank ordering, when it is known that the rank of an institution is one of the most difficult quantities to estimate.

He argues that a more suitable display is the funnel plot



EBMT Funnel plot

- In the funnel plot we plotted
 - x-axis: n
 - y-axis: $\hat{p} = x/n$
- Under H_0 :
 $\hat{p} \sim N(p_0, p_0(1 - p_0)/n)$
- Reject H_0 if
 $|\hat{p} - p_0| > 1.96 \sqrt{p_0(1 - p_0)/n}$
- Bounds do not depend on data and can be put into the plot before plotting the center results



- **x-axis: Expected ($E()$)**
 - $n p_0$
- **y-axis: Observed/Expected (O/E)**
 - $\frac{x}{n p_0} = \frac{\hat{p}}{p_0}$
 - Excess events over expected if center is performing according to benchmark
- **Test: reject H_0 if**

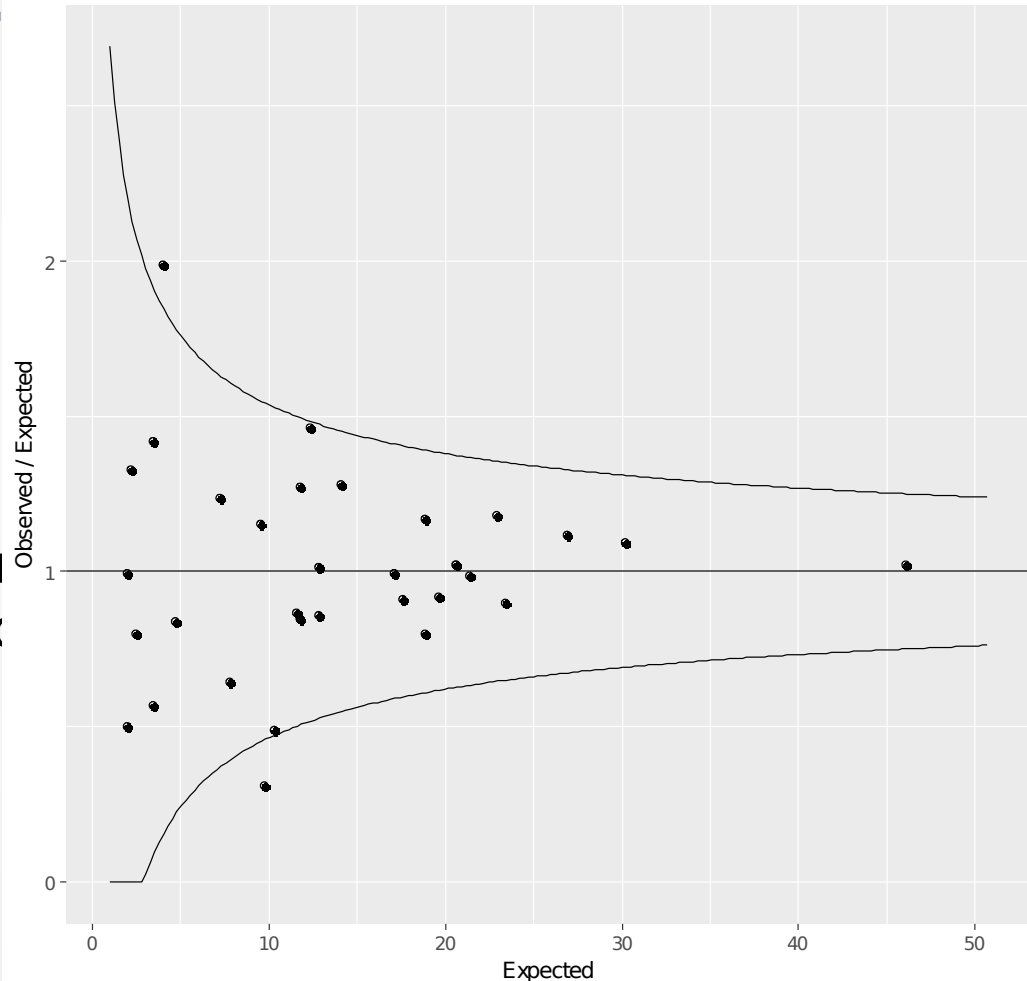
$$|\hat{p} - p_0| > 1.96 \sqrt{p_0(1 - p_0)/n}$$
- **Now becomes: reject H_0 if**

$$\left| \frac{O}{E} - 1 \right| > 1.96 \sqrt{(1 - p_0)/\sqrt{E}}$$
- Advantage: can be adapted to include case-mix
- Advantage: E can be adapted to include case-mix



EBMT Funnel plot

- Same type of plot
- This time with “Expected” on the x-axis
- And “Observed/Expected” (excess) on the y-axis
- “Expected” gives a measure of the amount of information in the data
 - The precision with which we have been able to estimate the excess



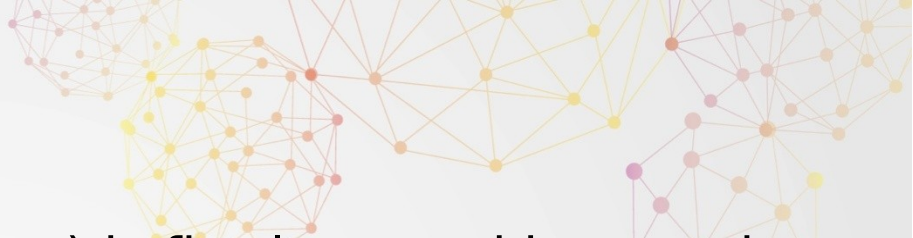


Survival outcomes

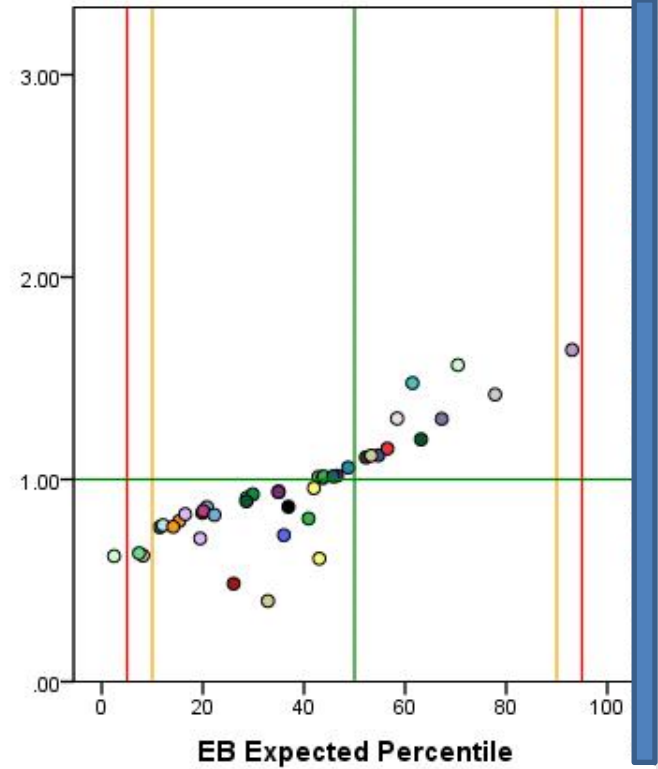
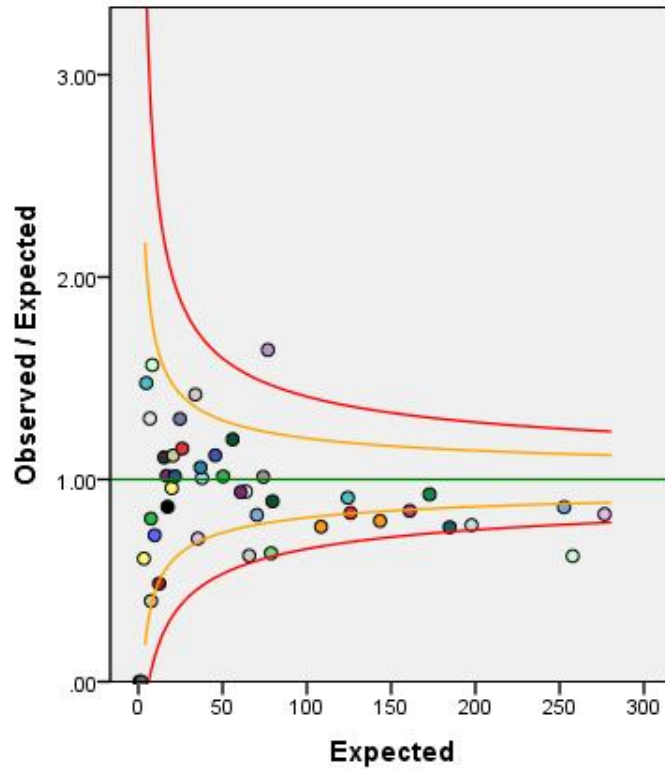
- Main question is what are and in the survival setting, with censored data?
- Data: for center i , subject j , outcome (t_{ij}, d_{ij}, x_{ij})
- Underlying model, accounting for case mix x_{ij}
$$h_{ij}(t) = h_0(t) \exp(\beta^T x_{ij})$$
- Define, for center i ,
- Under we have ,
$$D_i = \sum_j d_{ij}, E_i = \sum_j H_{ij}(t_{ij})$$
- Under H_0 we have $O_i \sim N(E_i, E_i)$



Remarks



- Justification of the approximation $Q_{\beta}(N, (E_i, SE_i))$ is firmly rooted in a counting process and martingale theory (Andersen, Bergman, Gill, Keiding, VII.2.2)
- Intuitive explanation of “Expected”: the number of events expected in a center, based on the number of patients, their characteristics and their follow-up and their patient characteristics
- Asymptotic test becomes: reject H_0 for center i if
- Asymptotic test becomes: reject for center i if
$$\left| \frac{\bar{E} - 1}{\sqrt{E}} \right| > \frac{1}{\beta}$$
- Bounds again do not depend on data, and can be put into the plot before plotting the center results
- In practice, β needs to be estimated, this is done under H_0

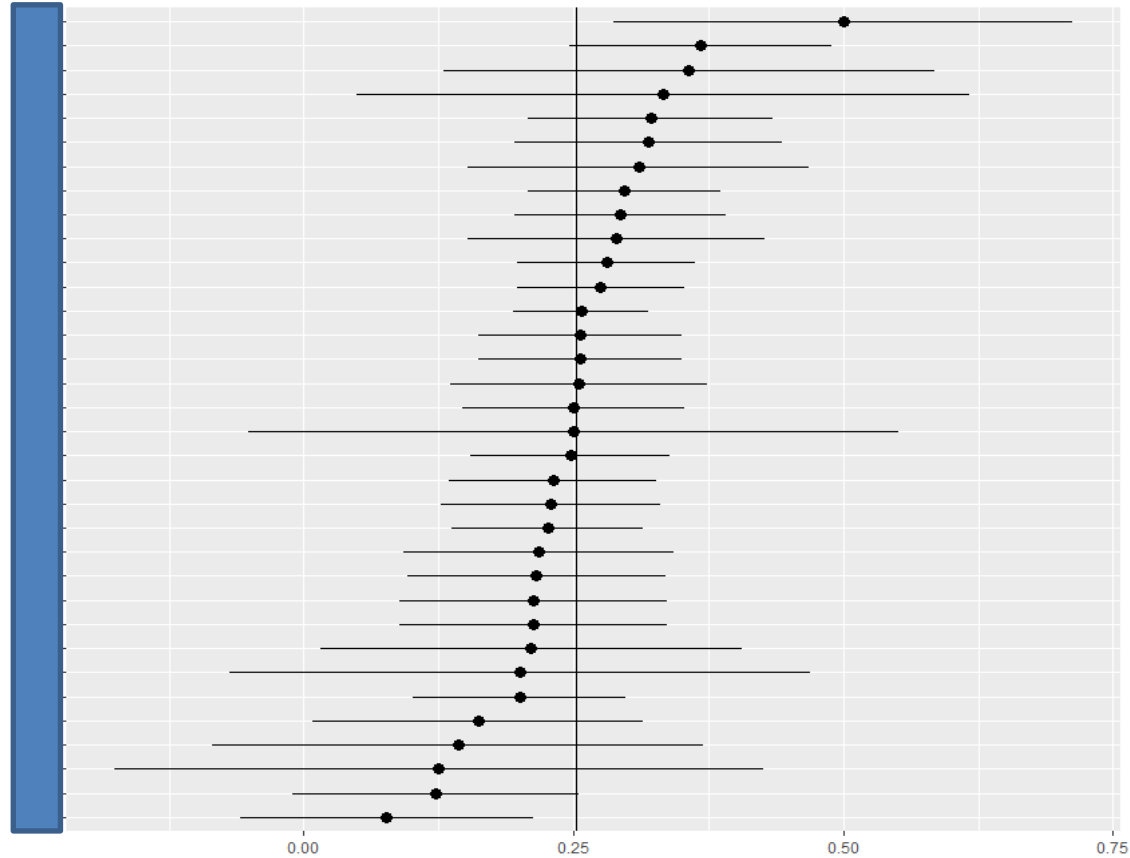




EBMT

Are there true differences?

- Suppose that each benefit has $p = 0.25$
- What would you expect?
- Could you see a picture like this?



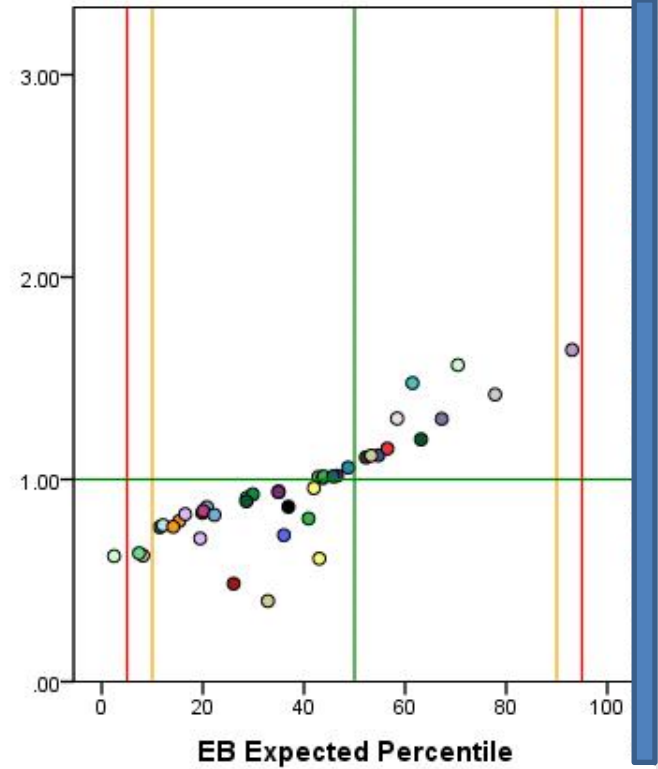
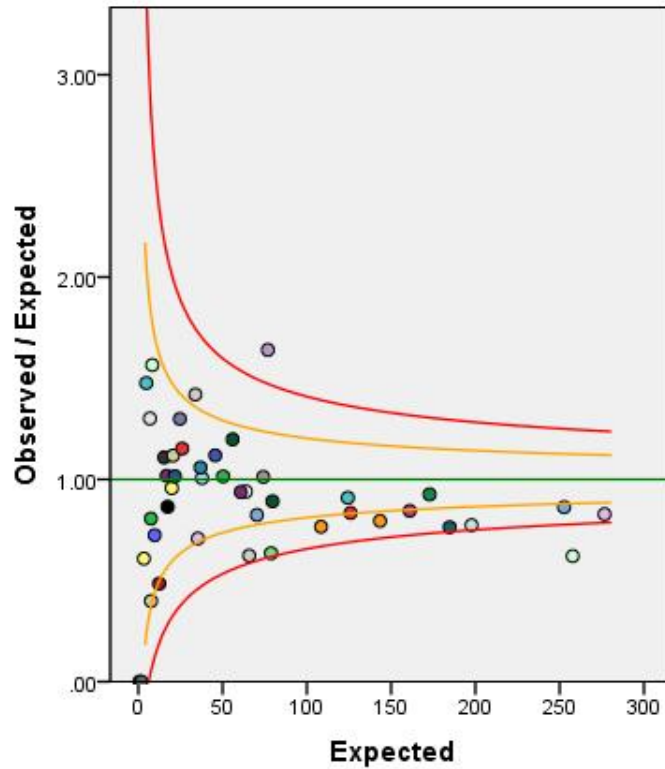


Ranking



- Ranking of centers is extremely dangerous and not recommended
- Even in a situation where all centers are performing similarly, **in the data** there will always be a best and a worst center
- No reason at all to expect in that case that the ranking will be the same next year
- More sophisticated methods needed to disentangle random from systematic differences between centers
- Instead of ranking propose so-called Empirical Bayes (EB) percentiles
- The EB percentile gives the expected rank accounting for case mix *and* chance fluctuations

It gets rid of the differences that are not significant





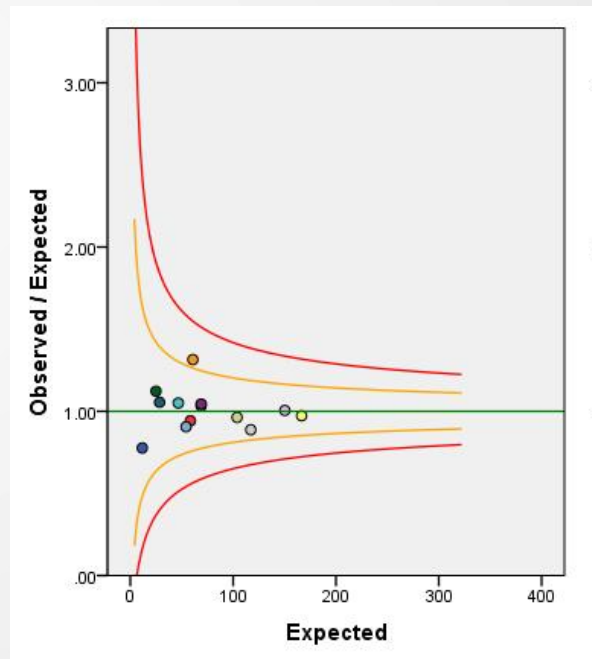
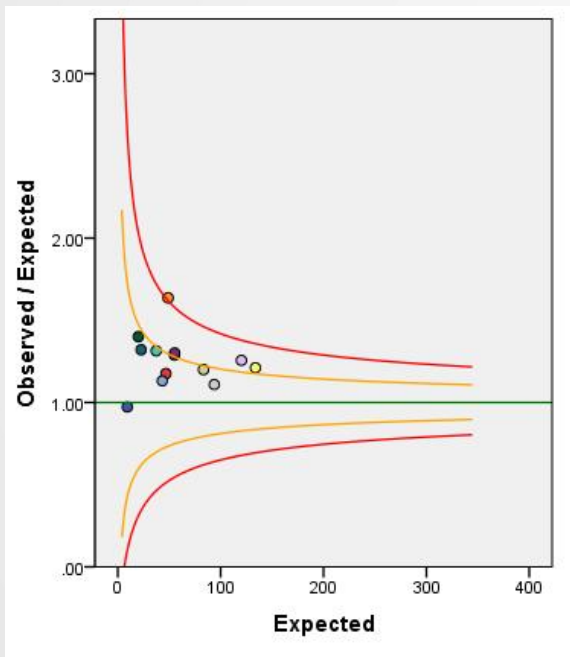
Target for benchmarking

- Target could be
 - A pre-set proportion or survival probability
 - Average in the same period of all centers, or
 - Average in the same period of all centers in the same country



ALLO, 12 months overall survival

- Center compared to other centers in Europe (left) or in its own country (right)



- In all of these outcomes we have to correct for case-mix
- This is because some specialized centers attract more serious patients
- Without correcting it would seem that these centers are performing badly
- Which variables to correct for, depends on
 - Clinical importance
 - Availability / completeness
 - Is the variable for case-mix a choice (consequence) of a center's strategy for transplantation?
 - o RIC and gender mismatch can be argued to at least partially be a **decision** by the treating physician and **not** a patient characteristic one is confronted with



- Essential for a successful benchmarking project
- This includes
 - Completeness of the registration of those risk factors determined to be used in the case-mix models
 - For survival data: completeness of follow-up
- Possible trap: perhaps all deaths are reported in a center, but follow-up of patients alive is lagging => bias (not in favor of the center)
- One can also benchmark completeness of patient data and of follow-up
 - Using similar methodology (reverse Kaplan-Meier)
 - No case-mix correction, because completeness of data and follow-up is generally not expected to depend on patient characteristics



Some general thoughts

- The ultimate goal is improvement of patient care
- Tool for centers to get more insight into their own performance
 - How are they doing in comparison with others, **after correcting for possible differences in case-mix**
- Trust and transparency is essential
 - In the procedure
 - In the models used
- We must be modest in what we claim
 - Case-mix correction model will not be perfect
 - But even an imperfect case-mix correction model is a hell of a lot better than a crude comparison